

NAME:
MATHS CLASS:
CURRENT GRADE:
TARGET GRADE:
TARGET SCORE:
EXAM SESSION:

## GCSE MATHEMATICS FOUNDATION REVISION BOOKLET



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Standard Form

## Prime Numbers

1. a) Express 32 and 56 as a product of prime factors.
b) By comparing the answers to (a) find the HCF of 32 and 56
2. By considering the product of prime factors, find the highest common factors of:
a) 45 and 99
b) 99 and 135
c) 45 and 135
3. Find the lowest common multiple of $\mathbf{6 0}$ and $\mathbf{7 2}$
4. Two lighthouses can be seen from the top of a hill. The first flashes once every 8 seconds, and the other flashes once every 15 seconds.
If they flash at the same time, how long will it be until they flash at the same time again?

## Exam Questions

Work out the Highest Common Factor (HCF) of 63 and 105.

Jenny is organising a barbecue.
There are 30 bread rolls in a pack.
There are 16 sausages in a pack.
She needs exactly the same number of bread rolls as sausages.
What is the smallest number of each pack she must buy?
You must show all your working

Answer ......................... packs of rolls
and packs of sausages

Write 108 as the product of its prime factors.
Give your answer in index form.


| REVIEW | REFLECTION / EVALUATION |
| :---: | :---: |
|  | The parts of this topic where I am confident are... |
|  | The areas of this topic that I still need to revise are... |
|  | Other comments/reminders... |

## Fractions, Decimals and Percentages

1. Find:
a) $\quad 3 / 4$ of $£ 120$
b) $\quad 4 / 5$ of 150 kg
c) $3 / 7$ of 210 cm
2. Find:
a) $\mathbf{2 5 \%}$ of $£ 360$
b) $35 \%$ of 800 kg
c) $95 \%$ of 460 cm
d) $\mathbf{2 4 \%}$ of $£ 95$
e) $\mathbf{3 2 \%}$ of $\mathbf{1 7 5 g}$
f) $\mathbf{9 8 \%}$ of $£ \mathbf{1 2 0}$
3. Gareth weighed 90 kg . He went on a diet to try to reduce his weight by $10 \%$.
a) How much did he try to lose?
b) He actually lost $17 \%$ of his body weight. How much was this?
4. A new born baby girl weighed 4 kg . In the first three months her weight increased by $60 \%$. How much weight had the baby gained?
5. Express these as percentages:
a) $\mathbf{1 2}$ out of $\mathbf{8 0}$
b) $\mathbf{2 7}$ out of $\mathbf{3 0}$
c) $\mathbf{2 6 0}$ out of $\mathbf{4 0 0}$
6. A glass of drink contains 50 ml of fruit juice and 200 ml of lemonade. What percentage of the drink is lemonade?

## Exam Questions

| Write $65 \%, 0.7$ and $\frac{16}{25}$ in order of size starting with the smallest. You must show your working. |  |
| :---: | :---: |
|  |  |
|  |  |
| Answer .................. | (Total 3 marks) |

Tom is 60 .
His daughter Fiona is $\frac{3}{5}$ of his age.
His grandson James is $\frac{4}{15}$ of his age.
How many years older than James is Fiona?
$\qquad$

| Work out the value of | $\frac{1}{4}+\frac{2}{3}$ |  |
| :---: | :---: | :---: |
| Answer $\qquad$ <br> (Total 2 marks) |  |  |
|  |  |  |

Work out
(a) $\frac{2}{5} \times \frac{1}{4}$

## Answer

(b) $\frac{3}{4}-\frac{1}{5}$

The table shows Ann's marks in two tests.

| Test | Mark |
| :---: | :---: |
| 1 | 60 out of 80 |
| 2 | 70 out of 100 |

In which test did Ann do better?
You must show your working.



| REVIEW | REFLECTION / EVALUATION |
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## Indices

1. What is the answer to the following:
a) V121
b) V169
c) $\quad \mathrm{V} 400$
d) $\quad$ v1
2. Evaluate the following:
a) $\quad 7^{2}$
b) $\quad 15^{2}$
c) $4^{3}$
d) $\quad 2^{3}$
3. Simplify the following expressions, giving your answer in index notation:
a) $3^{7} \times 3^{6}=$
b) $5^{6} \times 5^{4}=$
c) $\quad 11^{3} \times 11^{9}=$
d) $\quad 2^{5} \times 2^{3}=$
e) $\quad 7^{5} \div 7^{2}=$
f) $6^{4} \div 6^{2}=$
g) $\quad \frac{8^{12}}{8^{4}}=$
h) $\quad \frac{7^{2}}{7^{6}}=$
4. Simplify the following expressions, giving your answer in index notation:
a) $\quad\left(2^{3}\right)^{4}=$
b) $\quad\left(5^{2}\right)^{4}=$
c) $\quad\left(3^{6}\right)^{7}=$
d) $\quad\left(4^{4}\right)^{4}=$
5. Simplify the following expressions, giving your answer in index notation:
a) $y^{3} x y^{4}=$
b) $\mathrm{a}^{6} \times \mathrm{a}^{9}=$
c) $\quad \mathrm{e}^{5} \div \mathrm{e}^{9}=$
d) $\quad\left(n^{4}\right)^{5}=$
6. Simplify the following expressions, giving your answer in index notation:
a) $\frac{x^{4} \times x^{5}}{x^{3}}=$
b) $\frac{y^{12} \times y^{6}}{y^{2} \times y^{7}}=$
c) $\quad\left(x^{3} \times x^{4}\right)^{5}=$

## Exam Questions

Glynn says that $\sqrt{16+9}$ is the same as $\sqrt{16}+\sqrt{9}$
Show that Glynn is wrong.
(a) Work out the value of $\quad \sqrt{25} \times \sqrt[3]{64}$

Answer $\qquad$
(b) (i) Write down the value of $9^{2}$.

Answer $\qquad$
(ii) Tick the box for the statement that is true.

The sum of the squares of two odd numbers is always odd

The sum of the squares of two odd numbers is always even
$\square$
$\square$

The sum of the squares of two odd numbers could be odd or even $\square$
Give an example to justify your choice.
$\qquad$
$\qquad$
(c) Here is another pattern.

| $2^{2}=4$ | and | $1 \times 3=3$ |
| :---: | :---: | :---: |
| $4^{2}=16$ | and | $3 \times 5=15$ |
| $6^{2}=36$ | and | $5 \times 7=35$ |
| $8^{2}=64$ | and | $7 \times 9=63$ |
| $10^{2}=100$ | and | $9 \times 11=99$ |

You are given that $88^{2}=7744$
Write down the value of $87 \times 89$
Answer
(a) Simplify

| REVIEW | REFLECTION / EVALUATION |
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Answer
(b) (i) If $y=-1$ which answer in part (a) is positive?

Answer
(ii) If $y=0.5$ which answer in part (a) has the greatest value?

Answer

## Ratio

1. Simplify the following ratios:
a) $5: 10$
b)
8:12
c) 6:27
d) 22:55
e) 4:12:60
f)
15:50:100
g) $\quad 8: 40: 2$
h) 51:17:34
2. Jennifer mixes 600 ml of orange juice with 900 ml of apple juice to make a fruit drink. Write the ratio of orange juice to apple juice in its simplest form.
3. In a school there are $\mathbf{8 5 0}$ pupils and $\mathbf{4 0}$ teachers. Write the ratio of teachers to pupils.
4. A map is drawn with the scale $1: 50,000$. calculate the actual distances, in km that the following lengths on the map represent.
a) 2 cm
b) $\quad 9 \mathrm{~cm}$
c) $\quad 30 \mathrm{~cm}$
5. On a map, a distance of 5 cm represents an actual distance of 15 km . Write the scale of the map in the form 1:n
6. Ben buys 21 football stickers for $\mathbf{8 4}$ p. Calculate the cost of:
a) 7 stickers
b) $\quad \mathbf{1 2}$ stickers
c) $\mathbf{5 0}$ stickers
7. 16 teams each with the same number of people enter a quiz. At the semi-final stage there are 12 people left in the competition. How many people entered the quiz?

## Exam Questions

Mohsin invests some money in a cash ISA (c) and in a savings account (s).
The ratio of the amounts of money invested is $\quad c: s=3: 7$
He invests $£ 3600$ in the cash ISA.
How much money does he invest altogether?

Divide $£ 7200$ in the ratio $2: 3: 7$
$\qquad$
Alex and Ben share $£ 520$ in the ratio 1:3
(a) How much does Ben receive?
$\qquad$
$\qquad$
$\qquad$
Answer $£$

The sizes of the interior angles of a quadrilateral are in the ratio

$$
3: 4: 6: 7
$$

Calculate the size of the largest angle.
$\qquad$

|  | REFLECTION / EVALUATION |
| :---: | :---: |
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|  |  |
|  |  |

## Number Problems - Exam Questions Only

Greg goes shopping with $£ 20$.
He spends $£ 5.60$ on his lunch.
He needs $£ 1.30$ for his bus fare
He sees this advert for shoes.

| Shoes |
| :---: |
| Normal Price $£ 15$ |
| Sale price $10 \%$ off normal price |

Does he have enough money to buy them?
You must show your working
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Sam has $£ 1.65$
Vicki has 75p
How much must Sam give Vicki so that they each end up with the same amount?
$\qquad$
$\qquad$
$\qquad$

The shape of a flower bed is a cuboid as shown.

$1 \mathrm{~m}^{3}$ of soil weighs 1.25 tonnes
A gardener wants to fill the flower bed with soil as cheaply as possible. The table shows the costs for Company A and Company B.

| Company A | $£ 49.50$ per tonne | Delivery $£ 30$ |
| :--- | :--- | :--- |
| Company B | 10 tonnes for $£ 430$ <br> then $£ 67.50$ per extra tonne | Delivery free |

Which company should she use and how much will it cost?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer Company
$\qquad$

A supermarket sells jars of coffee of the same brand in two different sizes.
Regular
Large


Which jar gives the better value for money? You must show your working.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
Answer

Here are instructions for cooking a turkey.
Cook for 15 minutes at $220^{\circ} \mathrm{C}$
Reduce the oven temperature to $160^{\circ} \mathrm{C}$ and cook for 40 minutes per kilogram.

Kirsty is going to cook a 7 kilogram turkey.
She wants to take it out of the oven at 12:45 pm.
At what time must she start to cook it?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Three shops advertise the same luxury chair. Each shop has a special offer.

## Shop A

Chair - normal price £600
Special Offer - 30\% off normal price

## Shop B

Chair - normal price $£ 550$
Special Offer - $\frac{1}{5}$ off normal price


## Shop C

Chair - normal price £820

Special Offer - buy one get one free
(a) Mutasem wants to buy two of these luxury chairs.

At which shop is the price of the two chairs the cheapest?
You must show your working.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
Answer: Shop


## Area and Perimeter - Exam Questions Only

You have a square piece of paper which is folded in half to form a rectangle as shown.


The perimeter of the rectangle is 39 centimetres.
What is the area of the square you started with?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

In the diagram below, $P Q=10.8 \mathrm{~cm}, Q R=11.6 \mathrm{~cm}, R S=17.5 \mathrm{~cm}$ and $P S=9.5 \mathrm{~cm}$. The angles at $P$ and $S$ are $90^{\circ}$


Calculate the area of $P Q R S$.
$\qquad$
$\qquad$
$\qquad$

The base of a triangle is 36 mm .
The height of the triangle is 32 mm .

(a) Work out the area of the triangle.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
Answer $\qquad$ $\mathrm{mm}^{2}$
(b) The dimensions of the triangle are given to the nearest millimetre.

Write down the least possible length of the base of the triangle.

> Answer
mm
(a) The diagram shows a rectangle.


Work out the area of the rectangle.
State the units of your answer.
$\qquad$
$\qquad$
$\qquad$
(b) The diagram shows a rectangle made from two congruent shapes $A$ and $B$.

(i) Write down the mathematical name of shape $B$. Answer
(ii) Explain how you could work out the area of shape $B$.
$\qquad$
$\qquad$
$\qquad$
$A B C D$ is a quadrilateral.

(a) Write down an expression for the perimeter of the quadrilateral in terms of $x$ and $y$. Simplify your answer.
$\qquad$
$\qquad$
Answer $\qquad$
(b) When $x=4 \mathrm{~cm}$, the perimeter of the quadrilateral is 68 cm .

Find the value of $y$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
Answer cm


What is the area of the shaded square $P Q R S$ ?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$ $\mathrm{cm}^{2}$

| REVIEW | REFLECTION / EVALUATION |
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## Circles

1. Calculate the circumference and area of a circle where the diameter ( $D$ ) is:
a)
$D=10 \mathrm{~cm}$
b)
$D=11 m$
c)
$D=12.3 \mathrm{~mm}$
2. Calculate the circumference and area of a circle where the radius $(R)$ is:
a) $\quad R=12 \mathrm{~cm}$
b) $\quad R=8.2 \mathrm{~m}$
c) $\quad R=12 \frac{1}{4} \mathrm{~mm}$

## Exam Questions

Work out the circumference of a circle of diameter 10.5 cm .

$\qquad$
$\qquad$
$\qquad$

The radius of the semicircle is 10 cm .


Not drawn accurately

Work out the area of the semicircle.
State the units of your answer.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

A circle fits inside a semicircle of diameter 10 cm as shown.


Calculate the shaded area.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
Answer .................................................... $\mathrm{cm}^{2}$

| REVIEW | REFLECTION / EVALUATION |
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## 3D Shapes

1. Calculate the volume of the following 3 D shapes:
a)

b)

c)

d)


## Exam Questions


(a) The school hall is 30 m long, 12 m wide and 4 m high.
(i) Calculate the volume of the hall.
$\qquad$
$\qquad$
$\qquad$
$\qquad$ $\mathrm{m}^{3}$
(ii) Calculate the total area of the four walls of the hall.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$$\mathrm{m}^{2}$

Centimetre cubes are fitted together to make a solid as shown on the left.


The solid is packed into a box as shown on the right.
The box is a cuboid.
Work out the volume of the box.

Answer
$\mathrm{cm}^{3}$

The diacram shows two boxes that are cuboids.
(b) The diagram shows a cylindrical water tank.

The cross-section of the tank is a circle of radius three metres.
The depth of water in the tank is 0.5 metres.


Not drawn accuratelly

Calculate the volume of water in the tank.
Give your answer in terms of $\pi$.
$\qquad$
$\qquad$
$\qquad$


| REVIEW | REFLECTION / EVALUATION |
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## Shapes - Interior/Exterior Angles

1. Calculate the size of the missing angles:
a)

b)

c)

d)

e)

f)

g)


## Exam Questions

(b) In the diagram, angle $x$ is $115^{\circ}$.


Explain why $P Q R$ is not a straight line.
$\qquad$
$\qquad$
$A B C$ is a triangle.
$D$ is a point on $A B$ such that $B C=B D$.

(a) Work out the value of $x$.
$\qquad$
$\qquad$
Answer degrees
(b) Work out the value of $y$.
$\qquad$
$\qquad$
Answer
degrees
(c) Does $A D=D C$ ?

Give a reason for your answer.
$\qquad$
$\qquad$
(a) Triangle $P Q R$ is isosceles.
$P Q=P R$.


Work out the value of $x$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$A B C$ is an isosceles triangle. $B C D E$ is a kite.


Work out the value of $x$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## $A B C D E$ is a regular pentagon.



## Not drawn accurately

Work out the value of $x$.
$\qquad$
$\qquad$
$\qquad$

## Transformations - Exam Questions Only



The diagram shows two identical shapes $A$ and $B$.


Describe fully the single transformation which takes shape $A$ to shape $B$.
$\qquad$
$\qquad$
$\qquad$

The diagram shows two identical shapes, $A$ and $B$.


Describe fully the single transformation which takes shape $A$ to shape $B$.
$\qquad$
$\qquad$
$\qquad$
(a)

(i) Describe fully the single transformation that takes the shaded triangle to triangle $A$.
$\qquad$
$\qquad$
(ii) On the grid above translate the shaded triangle by 2 squares to the right and 4 squares down.

The vertices of triangle $T$ are (1, 1), (1,2) and (4, 1).


Enlarge triangle $T$ by scale factor 2 , with $(0,0)$ as the centre of enlargement.
(b) Triangle P is an enlargement of the shaded triangle.

(i) What is the scale factor of the enlargement?

Answer
(ii) What is the centre of enlargement?
Answer (........................, .......................)

| REVIEW | REFLECTION / EVALUATION |
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## Parallel Lines (Angles) - Exam Questions Only

$A C$ and $D G$ are parallel lines.
Angle $A B E=40^{\circ}$
Angle $B F G=110^{\circ}$


Not drawn accurately
(a) Explain why angle $B E F$ is $40^{\circ}$
$\qquad$
$\qquad$
(b) Show, giving reasons, that triangle $B E F$ is isosceles.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
In the diagram $A B$ is parallel to $D C$.
Angle $A B C=70^{\circ}$
Angle $A C D=55^{\circ}$


Show that triangle $A B C$ is isosceles.
You must give reasons in your working
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$A B C$ is a straight line.
Angle $A B E$ is twice the size of angle $C B E$.


Not drawn accurately

Show that $B E$ is not parallel to $D C$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

In the diagram $A B$ and $C D$ are parallel.


Not drawn accurately
(a) Write down the value of $x$.
$\qquad$
(b) Work out the value of $y$.
$\qquad$
$\qquad$
$A B$ is parallel to $C D$.


Work out the value of $t$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

| REVIEW | REFLECTION / EVALUATION |
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## Algebra (Simplification and Factorisation etc...)

1. Expand the following:
a) $3(a+1)=$
b) $\quad 2(5 x-12)=$
c) $6(2 y-5)=$
d) $-2(3 x-8)=$
e) $\quad-5(3-2 x)=$
f) $\quad-3(-4-x)=$
g) $x(x+1)=$
h) $a(4 a-5)=$
i) $6 y(5-2 y)=$
2. Expand and simplify the following:
a) $\mathbf{3 + 2 ( x - 8 )}$
b) $\quad 5(x+7)-12$
c) $\quad 4(x+2)+2(x-1)$
d) $2 x(x+1)-x(7-x)$
e) $3 x(x-2)-4(x-6)$
3. Factorise the following expressions:
a) $6 x+24=$
b) $12 \mathrm{x}-14=$
c) $3 \mathrm{a}-\mathbf{2 4}=$
d) $10+25 x=$
e) $3 x^{2}+6 x=$
f) $\quad 14 x^{2}+21 x=$
4. Expand and simplify the following:
a) $\quad(x+1)(x+6)$
b) $(2 x+1)(3 x-1)$
c) $(6 n+1)(4 n-2)$
5. Find the value of the following expressions when $a=2$ and $g=3$ :
a) 3a-g
b) $8 \mathrm{a}-5 \mathrm{~g}$
c) $\mathbf{3 1 + 9 a - 5 g}$
d) $6(7 a-g)$
e) $\mathbf{3 0}+\mathbf{2}(4 a+g)$
f) $\quad 9 \mathrm{~g}-(7-\mathrm{a})$

## Exam Questions

(a) Simplify $8 a-b+4 a-2 b$
$\qquad$
$\qquad$
(b) Multiply out $x(x+7)$
$\qquad$
Answer

## Complete this table.

| Expression | Value |
| :---: | :---: |
| $2 x$ | 8 |
| $5 x$ |  |
| $2 x+3 y$ | 5 |
| $y$ |  |
| $3 x-y$ |  |

$\qquad$
$\qquad$
$\qquad$
$\qquad$

## $A B C D$ is a quadrilateral.


(a) Write down an expression for the perimeter of the quadrilateral in terms of $x$ and $y$. Simplify your answer.
$\qquad$
$\qquad$

## Answer

$\qquad$
(b) When $x=4 \mathrm{~cm}$, the perimeter of the quadrilateral is 68 cm .

Find the value of $y$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(d) Factorise $15 t+25$
(b) Factorise $2 x^{2}-x$

Answer
(a) Expand and simplify $2(3 x-2)+4(x+5)$
$\qquad$
$\qquad$
$\qquad$
Answer

|  | REFLECTION / EVALUATION |
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|  |  |
|  |  |

## Sequences - Exam Questions Only

(a) The rule for the next term of a sequence is

Multiply the previous term by three and subtract one.
The first two terms of the sequence are 2 and 5 .
Write down the next two terms.
$\qquad$
$\qquad$ Answer 2
(b) The $n$th term of a different sequence is $5 n$.

The first term is 5
Write down the next three terms
Answer 5
(c) Work out the $n$th term of this sequence.

| 7 | 10 | 13 | 16 | 19 |
| :--- | :--- | :--- | :--- | :--- |

Answer
(b) Tom builds fencing from pieces of wood as shown below.


Diagram 1
4 pieces of wood


Diagram 2
$T$ pieces of wood


Diagram 3 10 pieces of wood

How many of pieces of wood will be in Diagram $n$ ?
$\qquad$
$\qquad$
$\qquad$
Answer $\qquad$

4 Here is a sequence of numbers.
$\begin{array}{lllll}35 & 30 & 25 & 20 & 15\end{array}$
4 (a) Write down the next number in the sequence.
Answer ....................................................................
(1 mark)
4 (b) Write down the rule for continuing the sequence.
Answer $\qquad$
4 (c) Which of the following expressions is the $n$th term of the sequence?
Circle the correct answer.

$$
5 n+30 \quad 5 n-40 \quad 30-5 n \quad 40-5 n
$$

$\qquad$
$\qquad$

4 (d) Here is a different sequence of numbers.

| 60 | 54 | 48 | 42 | 36 |
| :--- | :--- | :--- | :--- | :--- |

4 (d) (i) Both sequences are continued.
Write down two numbers which are in both sequences.
$\qquad$
$\qquad$
Answer $\qquad$ and $\qquad$
4 (d) (ii) Is -25 in both sequences? Give a reason for your answer.

$\qquad$
$\qquad$
$6 \quad$ Here is a sequence.
814
20
26 32

6 (a) Write down the rule for continuing the sequence.
$\qquad$
$\qquad$

6 (b) Write down the next two numbers in the sequence.
Answer $\qquad$ and $\qquad$ (1 mark)

6 (c) The $50^{\text {th }}$ term in the sequence is 302 .
What is the $48^{\text {th }}$ term in the sequence?
$\qquad$
$\qquad$

| REVIEW | REFLECTION / EVALUATION |
| :---: | :---: |
|  | The parts of this topic where I am confident are... |
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|  | Other comments/reminders... |

## Algebra (Graphs) - Exam Questions Only

(a) Complete the table of values for $y=2 x-1$

| $x$ | -1 | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | -3 |  | 1 |  | 5 |

$\qquad$
$\qquad$
(b) On the grid below, draw the graph of $y=2 x-1$ for values of $x$ from -1 to +3

19. On the grid, draw the graph of $y=4 x-2$

(a) Complete this table of values for $y=x^{2}-3$

| $x$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 6 | 1 |  | -3 | -2 | 1 | 6 |

$\qquad$
$\qquad$
(b) Draw the graph of $y=x^{2}-3$ for values of $x$ from -3 to +3 .



## Equations and Inequalities

1. Solve the following equations:
a) $x+6=2$
b) $3 x=-24$
c) $x-12=-4$
2. Solve the following equations:
a) $3 x+6=48$
b) $6 x+12=20$
c) $6 x-7=41$
d) $3(x-2)=12$
e) $\quad 5(5 x+1)=20$
f) $4(x+15)=60$
3. Solve the following equations:
a) $6 x+7=2 x+20$
b) $14-3 x=5$
c) $22-4 x=18-2 x$
4. Solve these inequalities:
a) $4 x+6 \leq 18$
b) $7 x+2 \geq-19$
c) $\quad 4(2 x-3) \geq-8$

## Exam Questions

(a) Solve $8 t-5=19$
(a) Solve the inequality $2 x+3 \geq 1$
$\qquad$
$\qquad$
(a) Solve the equation $\frac{x}{20}=-4$
$\qquad$
Answer $x=$
(b) Solve the equation $8 w-5=3 w+1$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

In the table below, the letters $w, x, y$ and $z$ represent different numbers. The total of each row is given at the side of the table.

| $w$ | $w$ | $w$ | $w$ |
| :---: | :---: | :---: | :---: |
| $w$ | $w$ | $x$ | $x$ |
| $w$ | $w$ | $x$ | $y$ |
| $w$ | $x$ | $y$ | $z$ |

24 28 25 23

Find the values of $w, x, y$ and $z$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$ $x=$ $\qquad$ $y=$ $\qquad$ $z=$ $\qquad$
(Total 4 marks)


Trial and Improvement - Exam Questions Only

Use trial and improvement to find a solution to the equation

$$
x^{3}+6 x=29
$$

Continue the table of results.
Give your solution to 1 decimal place.

| $x$ | $x^{3}+6 x$ | Comment |
| :---: | :---: | :---: |
| 2 | 20 | Too small |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |

$\qquad$
$\qquad$
$\qquad$
$\qquad$

## The equation

$$
x^{3}+2 x=60
$$

has a solution between 3 and 4

Use a trial and improvement method to find this solution. Give your answer correct to 1 decimal place. You must show all your working.

A solution of the equation $x^{3}-5 x=31$ lies between $x=3$ and $x=4$
Use trial and improvement to find this solution, to one decimal place.
The first trial is shown in the table.

| $x$ | $x^{3}-5 x$ | Comment |
| :---: | :---: | :---: |
| 3 | $27-15=12$ | Too small |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |

Answer $x=$
(3 marks)


## Pythagoras Theorem - Exam Questions Only

Work out length $A B$ as a decimal.


Calculate $X Z$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## The diagram shows a right-angled triangle.



Calculate the length $x$.
$\qquad$
Calculate the length $x$ in the triangle.

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Probability - Exam Questions Only

A bag contains 6 red pens, 69 black pens and 25 blue pens.
(a) Write down the number of red pens as a fraction of the total number of pens in the box.

Give your answer in its simplest form.
$\qquad$
$\qquad$
Answer $\qquad$
(b) What percentage of the pens are not black?

$$
\text { Answer .................................................. } \%
$$

(c) Circle a word from the list to describe the chance of each of the following events.
(i) A pen chosen at random from the box is red.

$$
\text { impossible unlikely evens likely } \quad \text { certain }
$$

(ii) A pen chosen at random from the box is not green.

$$
\text { impossible unlikely evens likely } \quad \text { certain }
$$

Here is a list of numbers.

| 5 | 7 | 5 | 6 | 4 | 9 | 8 | 10 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(a) Work out the median.

## Answer

(2)
(b) One of the numbers is chosen at random.
(i) What is the probability that the number is 5 ?

Answer
(1)
(ii) Put these events in order of likelihood starting with the least likely.

A The number is 5 .
B The number is even.
C The number is greater than 8 .
$\qquad$
$\qquad$
Answer $\qquad$

Ronan is designing a game.
He has two sets of discs laid face down on a table.
The first set of five discs are labelled 1, 3, 5, 7, 9 .
The second set of four discs are labelled $2,4,6,8$.
Players turn over one disc, at random, from each set and add the numbers together.
(a) Complete the table to show all the possible totals.

|  | 1 | 3 | 5 | 7 | 9 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 2 | 3 | 5 | 7 |  |  |
| 4 | 5 |  |  |  |  |
| 6 |  |  |  |  |  |
| 8 |  |  |  |  |  |

(b) What is the probability of getting a total less than six?

## Answer

$\qquad$
(c) Ronan uses the game to raise money for charity.

Each player pays 20 p to play the game.
If a player gets a total of exactly 13 they win a bar of chocolate.
It costs Ronan 50 p for each bar of chocolate.
If 100 people play the game, show that Ronan should expect to raise $£ 12.50$ for charity.
$\qquad$
$\qquad$

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## Representing Data (Graphs/Charts etc...) - Exam Questions Only


(b) The shopkeeper thinks that more women than men buy monthly magazines.

Does the data support this?
Show working to justify your answer.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

The table shows the races that 60 primary school pupils entered on their Sports Day They each entered one race.

| Race entered | Number of pupils |
| :---: | :---: |
| Egg and spoon | 18 |
| 3-legged | 20 |
| Sack | 12 |
| Obstacle | 10 |

(a) Draw and label a pie chart to represent the information in the table.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

(b) Work out the percentage of pupils who entered the egg and spoon race.
(c) The pupils in the obstacle race took these times in seconds.

| 23 | 36 | 18 | 29 | 44 | 39 | 36 | 54 | 43 | 41 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Draw an ordered stem and leaf diagram to show this information.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
Key: | 2 | 3 represents 23 seconds


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## Interpreting Data - Exam Questions Only

On her way to work Janice passes through four sets of traffic lights.
She records the number of times she stops at traffic lights each day.
The table shows her results for ten weeks.

| Number of stops each day | Frequency <br> (number of days) |
| :---: | :---: |
| 0 | 1 |
| 1 | 6 |
| 2 | 12 |
| 3 | 15 |
| 4 | 16 |

(a) Calculate the mean number of stops each day.

Answer
(b) Janice says that she stops at every set of traffic lights on most days.

She is wrong.
Explain why she is wrong
$\qquad$
$\qquad$
(c) On average, how many days per week does Janice work?

Answer

## Three whole numbers have a mean of 30 .

(a) The numbers are all different.

Write down three possible numbers.
$\qquad$
Answer $\qquad$ and $\qquad$ and $\qquad$
(b) Two numbers are equal and the third number is smaller than the other two. Find three possible numbers.
$\qquad$

Answer $\qquad$ and $\qquad$ and $\qquad$
(c) Two numbers are equal and the third number is half the size of the other two. Work out the three numbers.
$\qquad$
$\qquad$

A survey of the adults in Oldtown is carried out to find the age at which they hope to retire.
(a) Here is one of the questions.

(i) Write down one criticism of the question.
$\qquad$
$\qquad$
(ii) Write down one criticism of the response section.
$\qquad$
$\qquad$

Jeff wants to know the number of driving lessons he might need before he passes his driving test.
He also wants to know the number of times he might have to take his driving test before he passes.
He collects some data and shows it on this scatter graph.

(a) Jeff ignores one of the points on the scatter graph.

Circle this point and give a reason why it should be ignored.
Reason $\qquad$
(b) Draw a line of best fit on the scatter graph.
(c) Jeff has already failed his driving test three times after a total of 40 driving lessons.
(i) Estimate how many more driving lessons Jeff needs if he is to pass his driving test on the fourth attempt.
$\qquad$
Answer $\qquad$
(ii) Give a reason why this estimate might be unreliable.
$\qquad$
$\qquad$

A doctor wants to encourage her patients to take more exercise.
The doctor has approximately 500 patients.
She decides to do a survey about what exercise her patients take.
(a) This is a question in the survey.

Q Doyou
exercise?
A Tick a box

(i) Give a criticism of the question.
$\qquad$
$\qquad$
$\qquad$
(ii) Give a criticism of the response section.
$\qquad$
$\qquad$
$\qquad$
25. Caleb measured the heights of 30 plants.

The table gives some information about the heights, $h \mathrm{~cm}$, of the plants.

| Height $(h \mathbf{~ c m})$ of plants | Frequency |  |  |
| :---: | :---: | :--- | :--- |
| $0<h \leqslant 10$ | 2 |  |  |
| $10<h \leqslant 20$ | 8 |  |  |
| $20<h \leqslant 30$ | 9 |  |  |
| $30<h \leqslant 40$ | 7 |  |  |
| $40<h \leqslant 50$ | 4 |  |  |

Work out an estimate for the mean height of a plant.


